E = mc² Used in the Creation of the Most Massive Quark Yet Discovered!
Analysis of DZero (DØ) Data from Fermi National Accelerator Laboratory

Have you ever wondered how scientists determine the properties of particles so small we cannot see them with microscopes? How do scientists even know that atoms exist? This activity will help you understand how these particles can be found and their mass determined using indirect measurements.

You will use Einstein's famous equation and experimental DØ data, including data collected in 1995 from a special candidate event that is two-dimensional rather than three-dimensional, to determine the mass of the top quark, the most massive quark discovered.

While this event looks complex at first, notice the following characteristics in the diagram below:
1. A proton and antiproton collide to create a top-antitop pair that exists for a very short time.
2. Almost immediately the very massive top and antitop decay into the constituents that are known as their “signature.”
3. These include:
   - Four "jets" (large blasts of particles) that are the result of decays of W bosons and some less massive quarks. It is important to note that one of the jets will often contain a low-energy or "soft" muon. The soft muon helps identify the jet as a bottom quark jet.
   - A muon and a neutrino. (You can see them in the upper right part of the diagram.)

A Top Quark - Antitop Quark Event from the
D-Zero Detector at Fermilab

[Diagram of a top quark-antitop quark event with labeled particles and jets.]
The image below shows the collision for the event labeled **Run 92704 Event 14022**. Other top-antitop candidate events can be represented by similar diagrams but may not have exactly the same debris, going in the directions shown here.

![Image of collision](image.png)

A thumbnail image of data from **Run 92704 Event 14022**.

**What do we know?**

DØ data are shown as event displays like this one for event **Run 92704 Event 14022**. It shows the recorded momentum (in GeV/c) of the particle debris that came from the collision. Your class has four DØ event displays.

Can you identify the constituents of the top-antitop signature in event display? Look closely; the only information given about the neutrino is the magenta tower indicating its direction. While scientists can predict with confidence that a neutrino comes out of the collision, DØ cannot detect it. Still, a careful consideration of the momentum before the collision and after the collision may give you a clue about how much momentum the neutrino has!

1. Momentum is conserved.
2. The total momentum of the system is zero before the proton and antiproton collide.
3. Momentum is a vector.
4. These 2D events largely occurred in the plane of the paper on which the event display is printed.
5. Physicists know that with a careful choice of units, it is possible to equate momentum and energy similar to the way mass and energy are related. Specifically, the momentum of the collision debris has the same *numerical value* as the energy or mass of the particles. In other words, \( E \text{ (in GeV)} = p \text{ (in GeV)} = m \text{ (in GeV)} \) (Gigaelectron Volts). This shows, then, that the total energy that came from the two top quarks that were formed is equal to the *numerical sum* of all the momenta discovered in the collision.

**What tools do we need for our analysis?**

We need a notebook to record masses and decay types (dielectron or dimuon); ruler, protractor, pencil to make a *momentum vector diagram*. We need our data.

**What will we do?**

We will work in teams of two to determine the neutrino momentum and the mass of the top quark. We will share our results with the class. We will discuss the significance and develop claims based on our data and the class data.
What are our claims? What is our evidence?
Your results must include:
  • A value for the missing momentum of the neutrino.
  • A value for the mass of the top quark.

These results can help you make a claim that answers these questions:
  • How do scientists use conservation of momentum to determine the missing momentum carried away by the neutrino?
  • How do scientists use conservation of energy to determine the mass of the top quark?
  • Can you explain whether mass, energy and momentum are the same thing given that the units at high energy are the same?
  • Can you use the evidence from your class data to describe how scientists decide when to announce discoveries?
  • Can you describe how the properties of the neutrino make it impossible to directly detect the presence of a neutrino in the event plot?